## FOUN045 Mathematics for Commerce

## Section 1: General Information

1.1 Administrative Details

| Subject: | Mathematics for Commerce |
| :--- | :--- |
| Code: | FOUNO45 |
| Stream: | Commerce |
| Points: | 12 |
| Pre-requisite none but see notes below |  |

1.2 Subject Workload

| Number of timetabled hours <br> per week | Number of Personal study <br> hours per week | Total workload hours per <br> week |
| :--- | :--- | :--- |
| 4 | 5 | 9 |

### 1.3 Pre-requisites

Students are required to have undertaken a pre-requisite subject.

A FOUN045 student should have a very good mathematical background in number, basic algebra and graphing. Knowledge of calculus, probability and statistics is desirable, but not necessary.

Students who do not have a strong background in Mathematics are advised to do the Bridging Programme Mathematics for Commerce paper.

Alternatively, a student may be advised to enroll in the Extra Mathematics Programme.

### 1.4 Other resource requirements

List specialist facilities and/or equipment required for the delivery of this subject:

Scientific calculator/ access to blackboard/in class technology

## Section 2: Academic Details

### 2.1 Subject Overview

Mathematical problem solving is an important technique for the solution of problems in any area of society. This paper aims to develop the ideas and concepts from Mathematics in such a way that the student develops their problem solving techniques in Mathematics and can apply the processes to Commerce. This paper will give the student a sound knowledge of mathematical concepts and prepare them for the demands of 100-level Commerce, Mathematical and Statistical papers at the University of Otago.

### 2.2 Learning Objectives and Outcomes

Learning Objectives
By the end of the paper, successful students will be able to:

1. explore the use of formulae, relationships, equations, expressions and statistical techniques in a variety of contexts.
2. use number, algebra, probability, statistics and financial maths in different situations and interpret their results.
3. develop their mathematical skills in number, algebra, financial maths, probability, statistics and some curve sketching.
4. gain and demonstrate an understanding and appreciation of problem solving techniques in a variety of contexts.

## Overview of Learning Outcomes

## Topic 1 FINANCIAL MATHEMATICS

At the end of this topic, a student should be able to:
calculate rates
calculate currency conversions
solve hire-purchase problems
solve commission problems
identify and calculate quantities using the simple interest formula
identify and calculate quantities using the compound interest formula
use the simple interest and compound interest formulae to solve real-life problems
identify two types of depreciation and solve depreciation problems using the formulae
solve appreciation problems using a formula
calculate annual effective rates
define and understand a break-even point in Commerce
form and use cost equations
form and use revenue equations
solve break-even analysis problems graphically and algebraically
form price- demand equations
solve break even equations involving price-demand equations
optimise yields
use the Future Value of an Annuity formula to solve problems for a variety of contexts
use the Present Value of an Annuity Formula to solve problems for a variety of contexts solve a range of problems dealing with financial situations.

## Topic 2 PROBABILITY

At the end of this topic, a student should be able to:
define probability
calculate probabilities
use and understand correct probability notations
find the probability of the union, intersection and complement of events
calculate the odds for an event
use Venn diagrams to find all possible outcomes and calculate probabilities
use decision diagrams and tables to find all the possible outcomes and calculate the probabilities of events with replacements and without replacements
use two way tables to find all the possible outcomes and calculate the probabilities of events apply probability theory to a range of problems.

## Topic 3: STATISTICS

At the end of this topic, a student should be able to:
identify and classify data into categorical data and numerical data, discrete and continuous data organize and interpret categorical and discrete data using statistical graphs such as bar graphs, dual bar charts and pie charts
organize, draw and interpret continuous data using statistical graphs such as histograms, frequency polygons and cumulative frequency curves
summarise, numerically, graphically and using SPSS, and interpret a set of data using measures of central tendency such as mean, mode and median
summarise, numerically, graphically and using SPSS, and interpret a set of data using measures of dispersion - range, interquartile range, percentiles and standard deviation
compare and comment on sets of data using various statistics
describe a discrete and continuous random variable draw the probability distribution of a discrete random variable calculate the expectation of a discrete random variable describe and calculate conditions for a fair game describe the conditions needed a binomial distribution calculate probabilities and statistics using the binomial distribution describe the conditions for a normal distribution interpret the spread of data in a normal distribution curve
calculate z-scores in a standard normal distribution
explain the significance of the $z$-score value calculate probabilities using a normal distribution
estimate and interpret sample means
estimate and interpret sample variance and standard deviation
use a statistical package to describe and analyse data
estimate and interpret sample sizes
find the difference between two sample variances and standard deviations and comment on them
calculate the probability of sample means
use the Central Limit Theorem to test samples
identify unusual samples
use confidence intervals to describe samples and populations.

### 2.3 Subject Content

Topic 1: Financial Mathematics
Topic 2: Probability
Topic3: Statistics.

### 2.4 Teaching Method/Strategies

FOUN045 will consist of 12 lectures and 36 tutorials over 12 weeks. Each week consists of one lecture and three tutorials. Working in groups and independent study will be used in classes.

### 2.5 Assessment

| Assessment Type | When | Weighting | Learning Outcomes Assessed |
| :--- | :--- | :--- | :--- |
| Internal | Mid-Term Test Week 7 <br> Statistical assignment <br> Week 8-11 | $15 \%$ | Topic 1 Financial Maths |
| Final Examination | Week 13 | $10 \%$ | Topic 3 some |

### 2.5.1 Assessment Strategy

Formal Written Mid-Term Test (in week 7) Duration: 50 minutes Included: all work covered in topic 1.
The test will consist of two compulsory questions.

| Question | Type of | Marks allocation |
| :---: | :--- | :---: |
| 1 | 10 parts, short answer | 20 |
| 2 | $3-5$ parts worth equal <br> marks, problem solving | 30 |
| Total |  | 50 |

Assignment: Statistics and SPSS: Week 8-11: students will be issued with a problem solving investigative exercise covering the topic Statistics. They are expected to answer the assignment questions using the correct statistical language with the correct use of the software package SPSS. Students should produce their work to a high standard. Students will have about two weeks to complete the assignment.

### 2.5.2 Hurdle Requirement

In order to pass this paper, students must obtain an overall mark of 50\% (C-) or better.

### 2.5.3 Assessment Details

| Assessment | Content/ Format | Time | Details |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Internal <br> Assessment mid term test | all work covered in topic 1 Financial Maths | 50 minutes | See above |  |  |
| Internal <br> Assessment <br> Statistics <br> Assignment | Written assignment | Over 3-4 weeks | See above |  |  |
| Final Examination | all work covered in topic 2 Probability and 3 Statistics | 2 hours | The examination will consist of four compulsory questions. |  |  |
|  |  |  | Question | Type | Marks allocation |
|  |  |  | 1 | 10 parts, short answer, 4 marks each | 40 |
|  |  |  | 2-4 | 3 problem solving context questions, worth 20 marks each. | 60 |
|  |  |  | Total |  | 100 |

### 2.6 Prescribed and Recommended Reading

Prescribed Text: none. Use Student Workbooks
Recommended Reading: none prescribed
Websites: none prescribed
3. Subject Details

See learning outcomes above

| Week | Lecture (1 hour) | Tutorial (1 hour) | Tutorial (1 hour) | Tutorial (1 hour) |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Introduction to paper and Topic 1 <br> Financial <br> Mathematics <br> Simple Interest and hire purchase | Using the calculator | Rates and currency conversions | Simple Interest <br> Set homework: Interest |
| 2 | Compound interest and AER | Hire-purchase | Compound Interest | Working in groups: Commission |
| 3 | Break-even analysis, linear | AER | Break Even analysis 1: Cost and Revenue equations | Break-even analysis 2 Use of st line graphs <br> Set Homework: <br> Appreciation <br> Depreciation |
| 4 | Price- demand analysis | Break Even analysis 3: price demand eqns | Break Even analysis 4: Optimising Yields use of quadratic graphs | Working in groups Optimising Yields |
| 5 |  <br> Present Value of an <br> Annuity | Future Value of an Annuity | Present Value of an Annuity | Revision or catch up |
| 6 | Topic 2 Probability | Intersection and union of events <br> Revision for test | Complement of events, odds of an event <br> Revision for test | Revision or catch up |
| 7 | Mid term tests Test (15\%) | Mid term tests | Successive Events and Decision Diagrams | Use of Two way tables |
| 8 | Topic 3 Statistics <br> Types of Data, Measures of Statistics | Measures of Central Tendency 1 | Measures of Central <br> Tendency 2 <br> Assignment: Statistics and SPSS issued and details | Working in groups: Statistical Graphs |
| 9 | Discrete Probability distribution, Binomial | Measures of Spread 1 | Measures of Spread 2 | Discrete Distributions Assignment queries |
| 10 | Normal ditribution | Binomial Distribution <br> Assignment queries | Normal Distribution <br> Tables <br> Assignment queries | Normal Distribution <br> Applications <br> Assignment queries |
| 11 | Estimation and Confidence intervals Assignment: due (10\%) | Estimation 1 | Estimation 2 | Estimation 3 |
| 12 | Confidence intervals | Confidence intervals | revision | revision |

